## Roll No.

Total No. of Printed Pages : 5

## Code No. : BC-200

Online Annual Examination, 2022

## B.C.A. Part I, II, III BRIDGE COURSE

Time : Three Hours ]
[ Maximum Marks : 50
Note : Section ' $A$ ', containing 10 very short answer type questions, is compulsory. Section ' $B$ ' consists of short answer type questions and Section ' $C$ ' consists of long answer type questions. Section ' $A$ ' has to be solved first.

## Section 'A'

Answer the following very short answer type questions in one or two sentences. $\quad \mathbf{1} \times \mathbf{1 0}=\mathbf{1 0}$

1. Write the first 3 terms of the sequence which is defined by :

$$
a_{n}=\frac{n}{n^{2}+1}
$$

2. Convert the following angle in radian measurement : $70^{\circ}$
3. Write the series of $\log (1+x)$.
4. Write the $8^{\text {th }}$ term of the series $(1+x)^{11}$.
5. Find the coefficient of $x^{5}$ in $(x+3)^{8}$.
6. On which axis do the following points lie :
(a) $(-5,0)$
(b) $(6,0)$
7. Find the mode of the following :
$12,13,17,18,11,13,21,1913$.
8. Define Identity matrix.
9. Arithmetic mean of $4,7, x$ and 9 is 7 . Find the value of $x$.
10. Write the conditions for two lines are perpendicular to each other.

## Section ' $B$ '

Answer the following short answer type questions with word limit 150-200.
$3 \times 5=15$

1. If the $6^{\text {th }}$ term of a GP is 32 and its $8^{\text {th }}$ term is 128 , then find the value of the common ratio.

## Or

Find the value of $x$ and $y$ from the following equation :

$$
2\left[\begin{array}{cc}
x & 5 \\
7 & y-3
\end{array}\right]+\left[\begin{array}{rr}
3 & -4 \\
1 & 2
\end{array}\right]=\left[\begin{array}{cc}
7 & 6 \\
15 & 14
\end{array}\right]
$$

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2. Prove that :

$$
\frac{{ }^{n} C_{r}}{{ }^{n} C_{r-1}}=\frac{n-r+1}{r}
$$

Or
If $\frac{e^{2 y}-e^{-2 y}}{2^{2 y}+e^{-2 y}}=\sin \alpha$, then find the value of $y$.
3. If $\operatorname{cosec} A=2$, find the value of $\frac{1}{\tan A}+\frac{\sin A}{1+\cos A}$.

## Or

Solve : $\tan ^{-1} 2 x+\tan ^{-1} 3 x=\frac{\pi}{4}$.
4. Find the focal distance of the point $P(2,0)$ on the ellipse $3 x^{2}+4 y^{2}=12$.

## Or

Find the focus of the parabola $y=x^{2}-2 x+3$.
5. The mean of the 5 numbers is 27 . If one of the number is excluded, the mean becomes 25. Determine excluded number.

## Or

Obtain the median for the following frequency distribution :


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## Section ' $\mathbf{C}$ '

Answer the following long answer type questions with word limit 300-350. $5 \times 5=25$

1. Find the partial fraction of the function :

$$
f(x)=\frac{1}{x^{2}-6 x+8}
$$

Or
Find the inverse of : $\left[\begin{array}{rrr}1 & 3 & -2 \\ -3 & 0 & -5 \\ 2 & 5 & 0\end{array}\right]$
2. Prove that ${ }^{2 n} C_{n}=2^{n} \frac{[1,3,5 \ldots \ldots .(2 n-1)]}{n!}$.

Or
If $(n+2)!=(1560) n!$, find $n!$
3. Evaluate $\sin \frac{\pi}{4} \cdot \cos \frac{\pi}{12}+\cos \frac{\pi}{4} \cdot \sin \frac{\pi}{12}$.

Or
Prove that $2 \tan ^{-1} x=\tan ^{-1}\left(\frac{2 x}{1-x^{2}}\right)$
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4. Find the equation of the acute angle between the lines:
$3 x+4 y-11=0$ and $12 x-5 y-2=0$
Or
Find the equation of the circle which touch the straight line $12 x-5 y+10$ and whose center is $(3,4)$.
5. Find the standard deviation of the following data:

| $x:$ | 4 | 8 | 11 | 17 | 20 | 24 | 31 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f:$ | 3 | 5 | 9 | 5 | 4 | 3 | 1 |
|  |  | Or |  |  |  |  |  |

The mean of 4, 7, 2, 8, 6 and 9 is 7. Find mean deviation about median of these observations.

